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# Huge-Scale Molecular Dynamics Simulation of Multi-bubble Nuclei

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## Outline

1. Introduction
2. Benchmark results
3. Cavitation
4. Future of HPC
5. Summary and Discussion

# Introduction (1/2)

## Gas-Liquid Multi-Phase Flow

Multi-Scale and Multi-Physics Problem

## Numerical Difficulties

Moving, Annihilation and Creation of Boundary

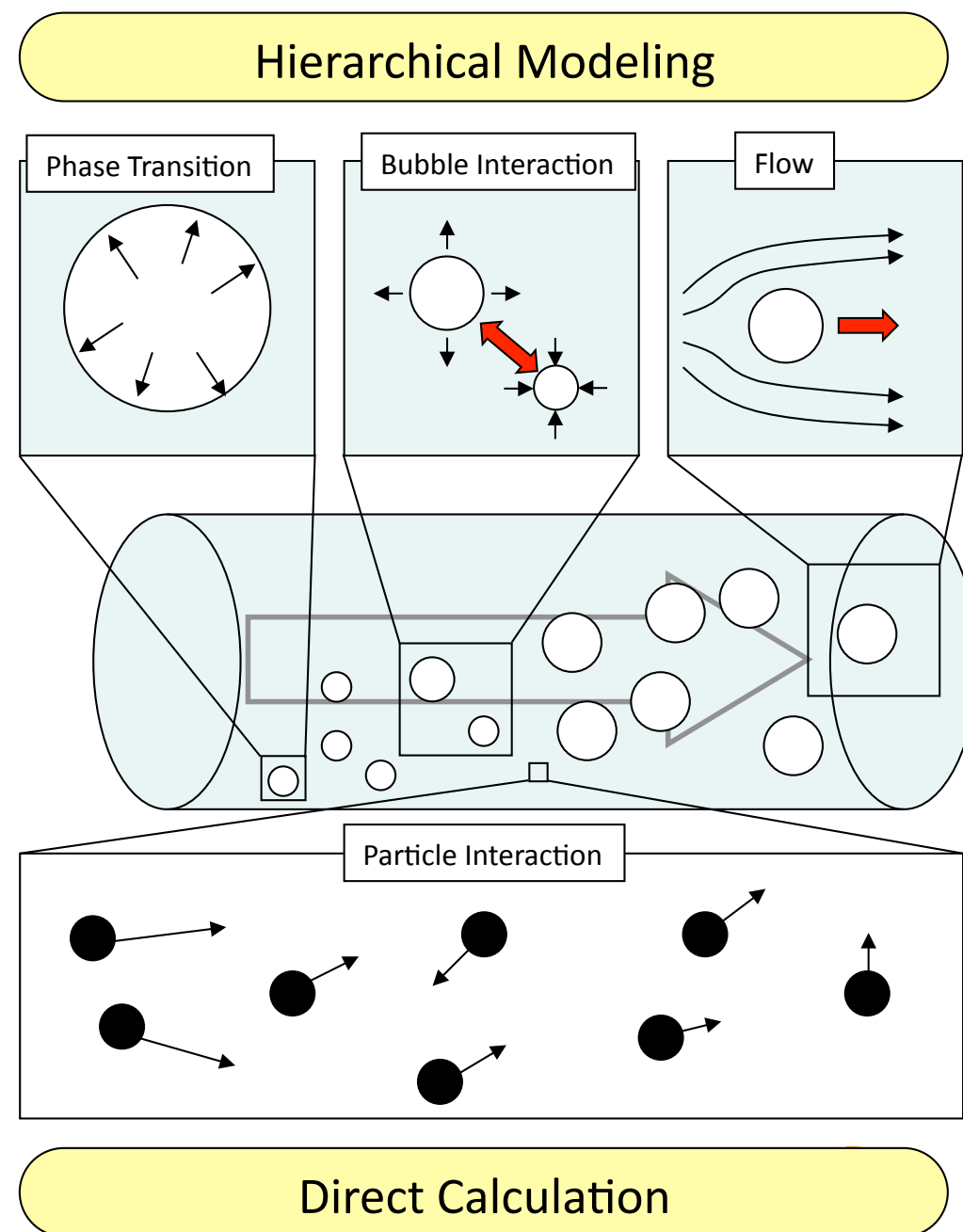
## Hierarchical Modeling

Divide a problem into sub problems  
Governing Equations for each scale

Artificial Hierarchy  
Validity of Governing Equation

 Direct Simulation

Movie



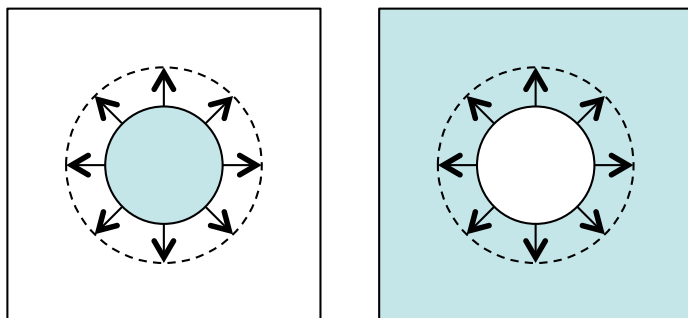
# Introduction (2/2)

## Classical Nucleation Theory

Classical nucleation theory (CNT) predicts a nucleation rate of clusters.  
OK for droplet nuclei, bad for bubble nuclei.

## Droplets and Bubbles

Additional work to create a bubble

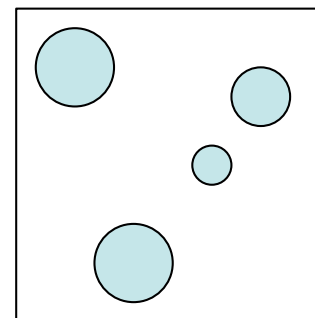


$$W = \gamma A - V\rho\Delta\mu - V\Delta P$$

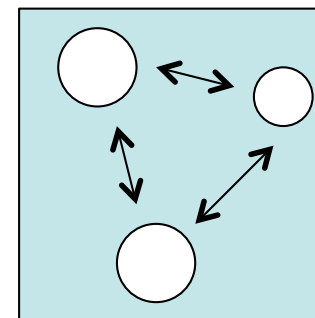
Same as Droplet

Work by Bubble

Interaction between clusters



Interact via gas (diffusive)



Interact via liquid (ballistic)

It is difficult to investigate microscopic behavior directly.



Huge scale molecular dynamics simulation  
to observe interaction between bubbles.



# Parallelization (1/3)

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## Simulation Method

Molecular Dynamics (MD) method with Short-range Interaction

## General Approach

MPI: Domain Decomposition

OpenMP: Loop Decomposition

```

DO I=1,N ←———— Loop Decomposition here
  DO J in Pair(I) ←———— or here
    CalcForce(I,J)
  ENDDO
ENDDO

```

## Problems

Conflicts on write back of momenta

→ Prepare temporary buffer to avoid conflicts

→ Do not use Newton's third law (calculate every force twice)

We have to thread parallelize other parts, such as pair-list construction.

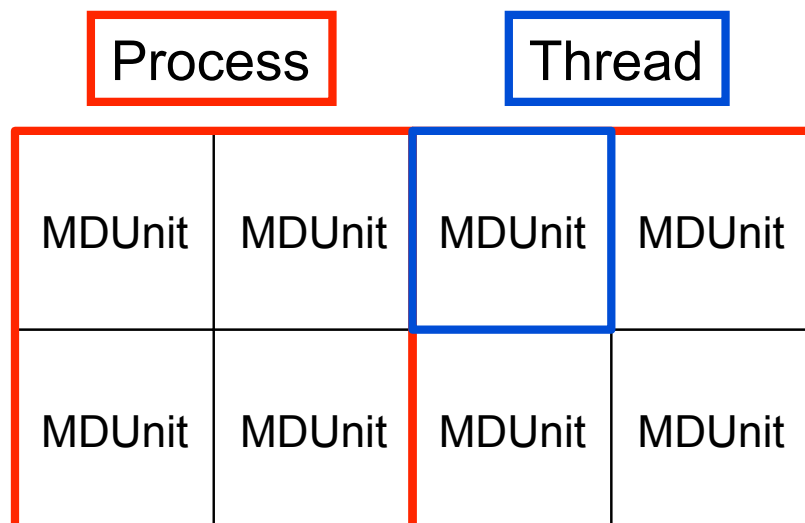
**We have to treat SIMDization and thread parallelization simultaneously.**



# Parallelization (2/3)

## Pseudo-flat MPI

Full domain decomposition for both intra- and inner-nodes.



MDUnit class :

Represent an OpenMP thread  
Responsible for calculation

MDManager class:

Represent an MPI process  
Responsible for communication

```
DO I=1,THREAD_NUM ← Loop parallelization
CALL MDUnit[i]->Calculate()
ENDDO
```

## Merits

It is straightforward to implement pseudo-flat MPI codes from flat MPI codes.

Memory locality is automatically satisfied. (not related to the K computer)

**We have to take care SIMDization only at the hot-spot (force calculation).**

→ We do not have to take care two kinds of load balance simultaneously.



# Parallelization (3/3)

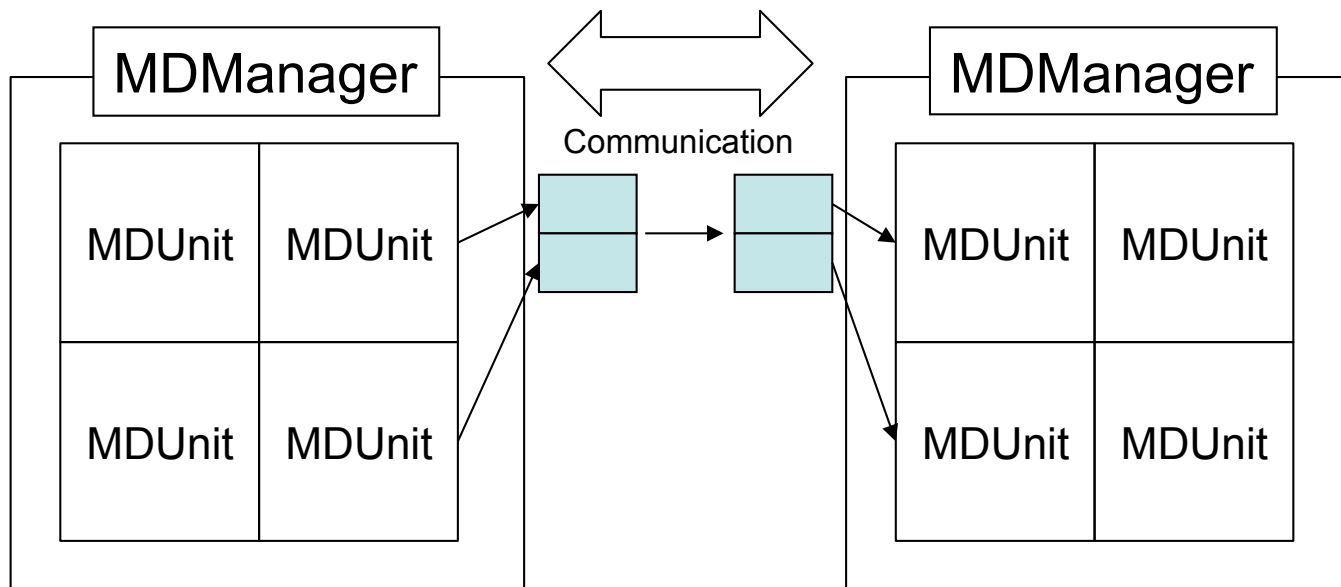
## Demerits

Two-level communication is required.

→ Limitation of MPI call in thread.

→ Data should be packed before being sent by a master thread.

It is troublesome to compute physical quantities such as pressure, and so on.



# Algorithms for MD

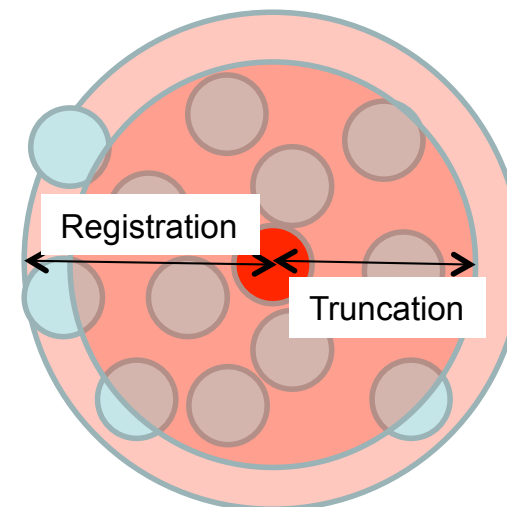
## Pair-list Construction

### Grid Search

$O(N)$  method to find interacting particle-pairs

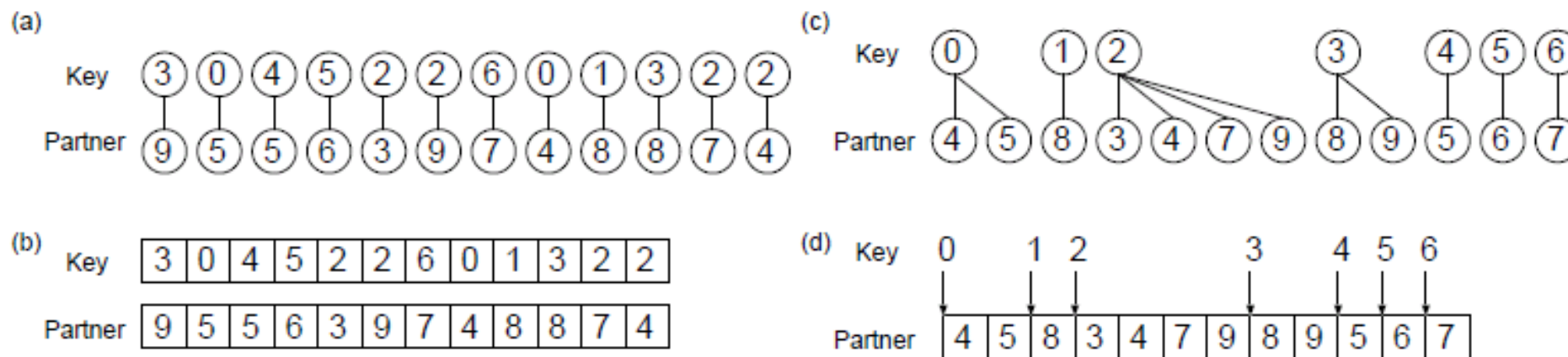
### Bookkeeping method

Reuse the pair-list by registering pairs in a length longer than truncation length.



## Sorting of Pair-list

Sort by i-particle in order to reduce memory access



# SIMDization

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## Non-use of Newton's third law

We find that store operations involving indirect addressing is quite expensive for the K computer.

- We avoid indirect storing by not using Newton's third law.  
Computations becomes double, but speed up is more than twofold.

The value of FLOPS is meaningless.

## Hand-SIMDization

Compiler cannot generate SIMD operations efficiently.

- We use intrinsic SIMD instructions explicitly. (`emmintrin.h`)

Divide instruction (`fdivd`) cannot be specified as a SIMD instruction.

We use a reciprocal approximation (`frcpd`) which is fast, but accuracy is only 8bit.

We improve the precision by additional calculations.

The loop is unrolled by four times to enhance the software pipelining.

You can see the source codes from: <http://mdacp.sourceforge.net/>





# Benchmark (1/3) - Conditions -

## Conditions

Truncated Lennard-Jones potential with cutoff length 2.5 (in LJ units)

Initial Condition is FCC and density is 0.5

Integration Scheme: 2<sup>nd</sup> order symplectic with  $dt = 0.001$

0.5 million particles on a CPU-core (4 million particles on a node)

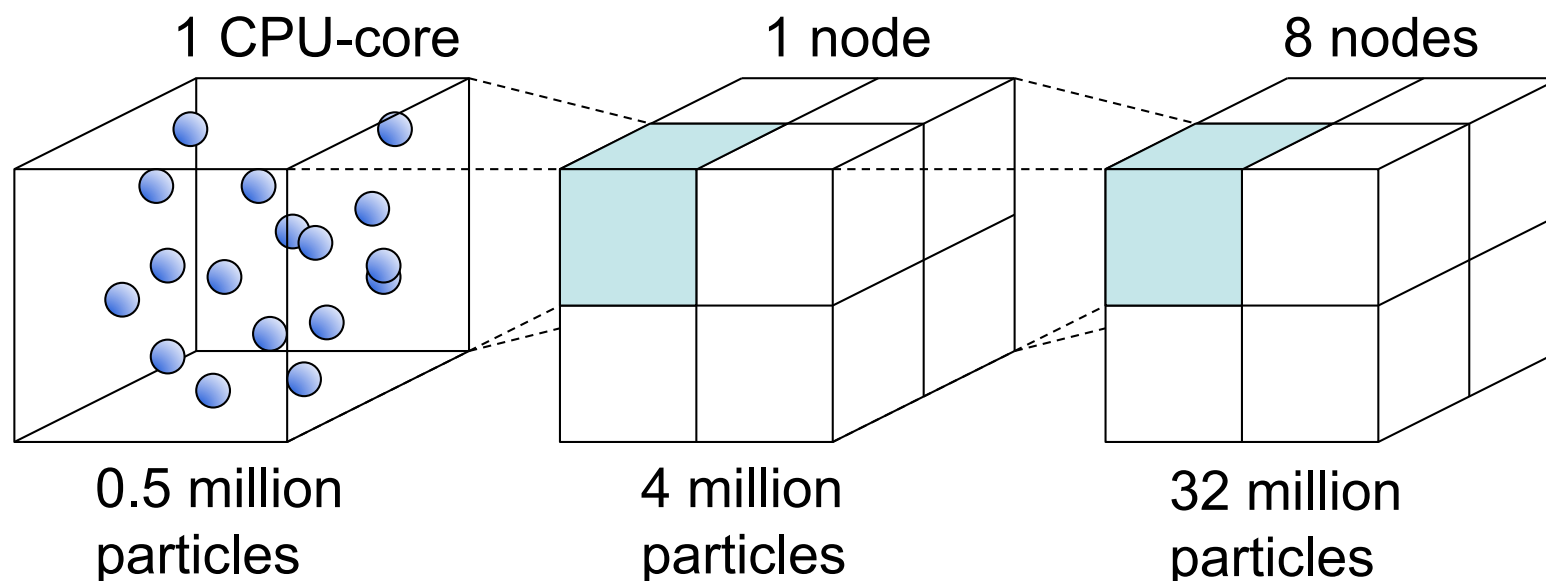
After 150 steps, measure time required for 1000 steps.

## Parallelization

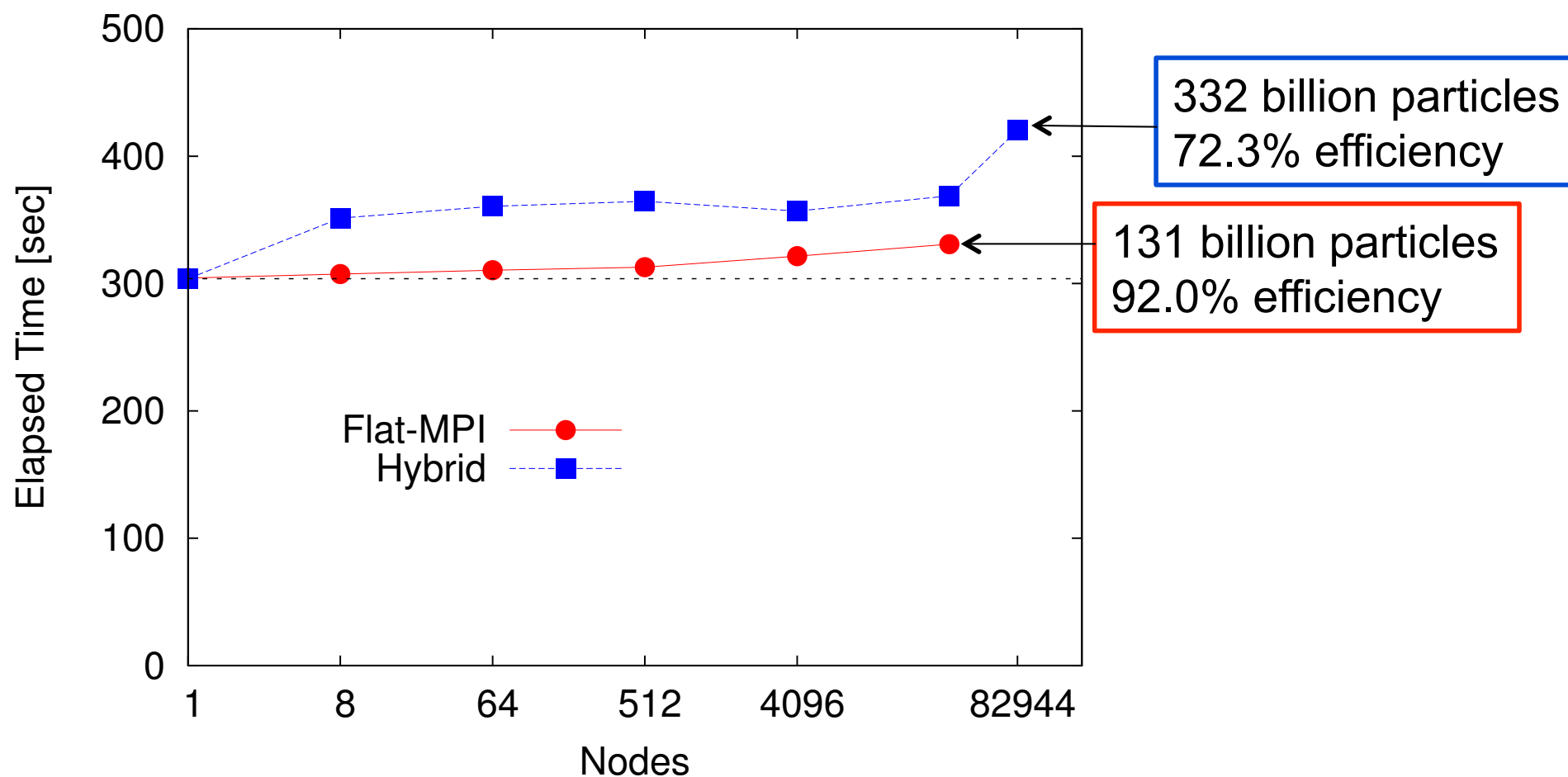
Flat MPI : 8 processes /node up to 32768 nodes (4.2 PF)

Hybrid : 8 threads/node up to 82944 nodes (10.6 PF)

Computations assigned to each core are perfectly identical for both scheme.



## Benchmark (2/3) - Elapse Time -



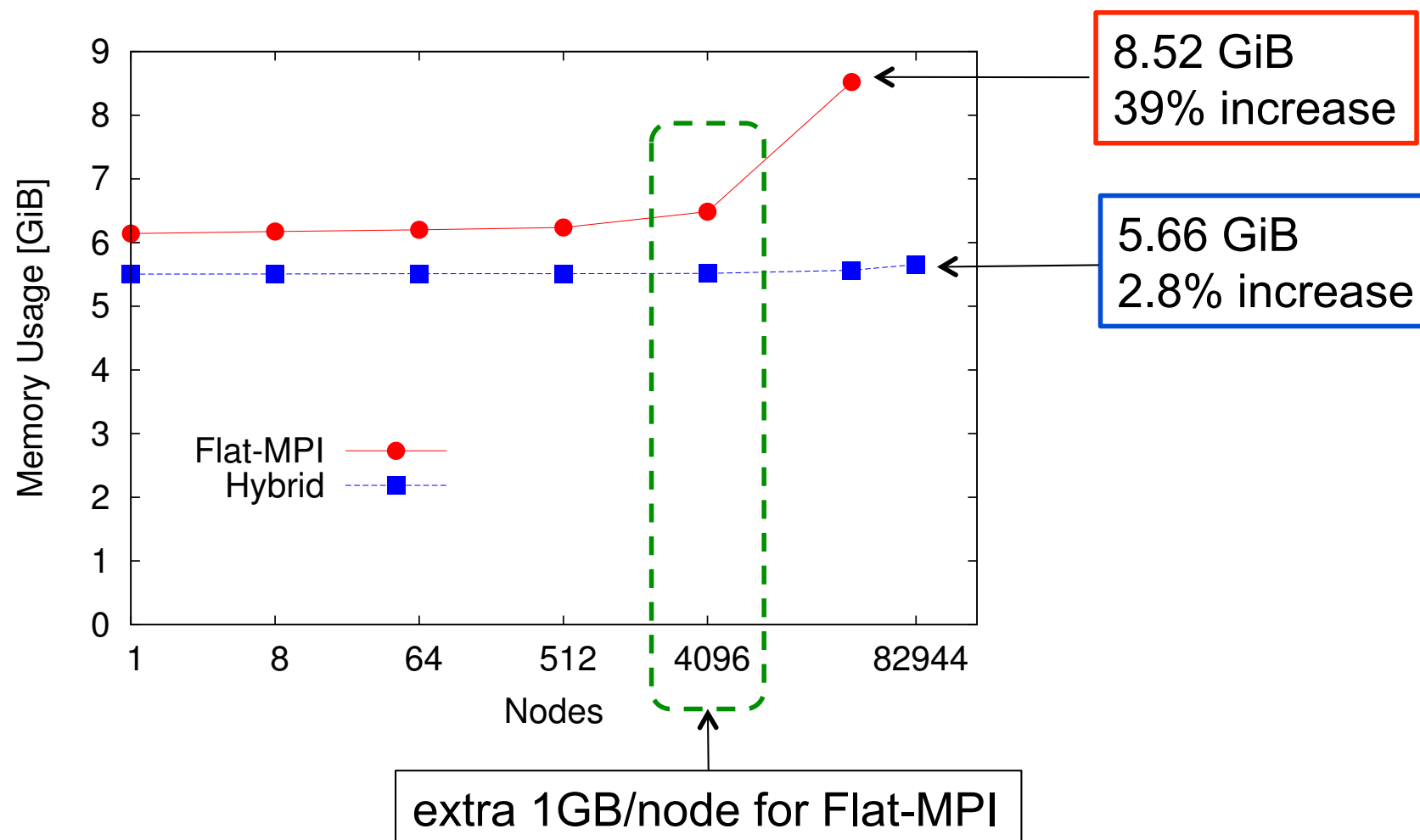
Nice scaling for the flat MPI (92% efficiency compared with a single node)

Performance of the largest run: 1.76 PFLOPS (16.6%)



## Benchmark (3/3) - Memory Usage -

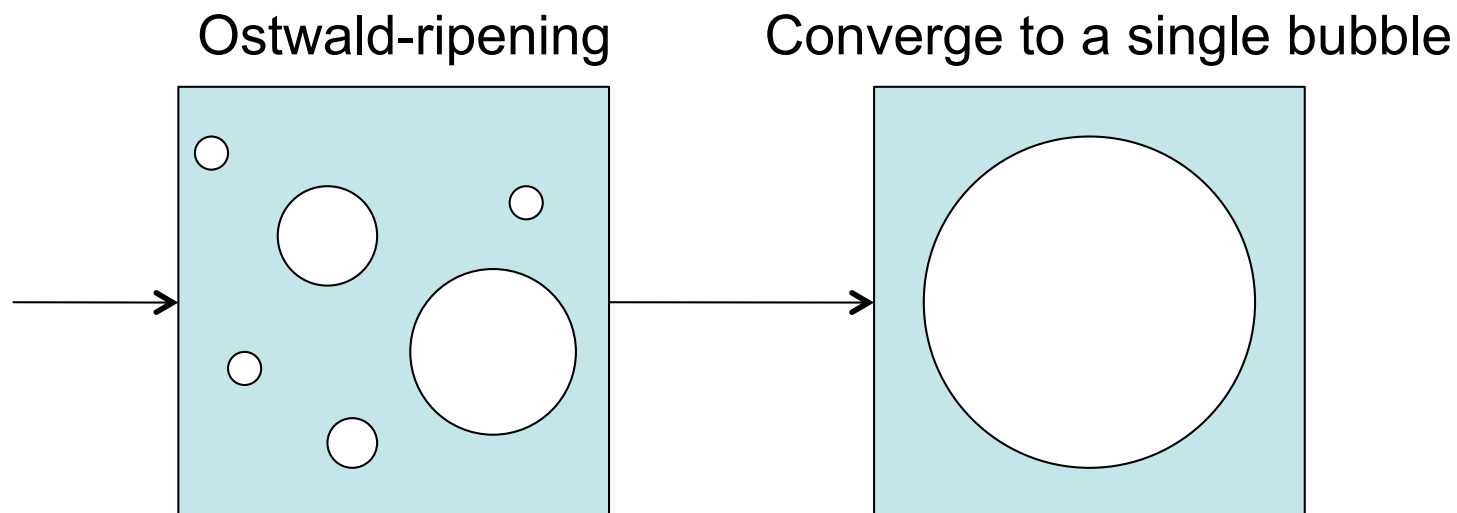
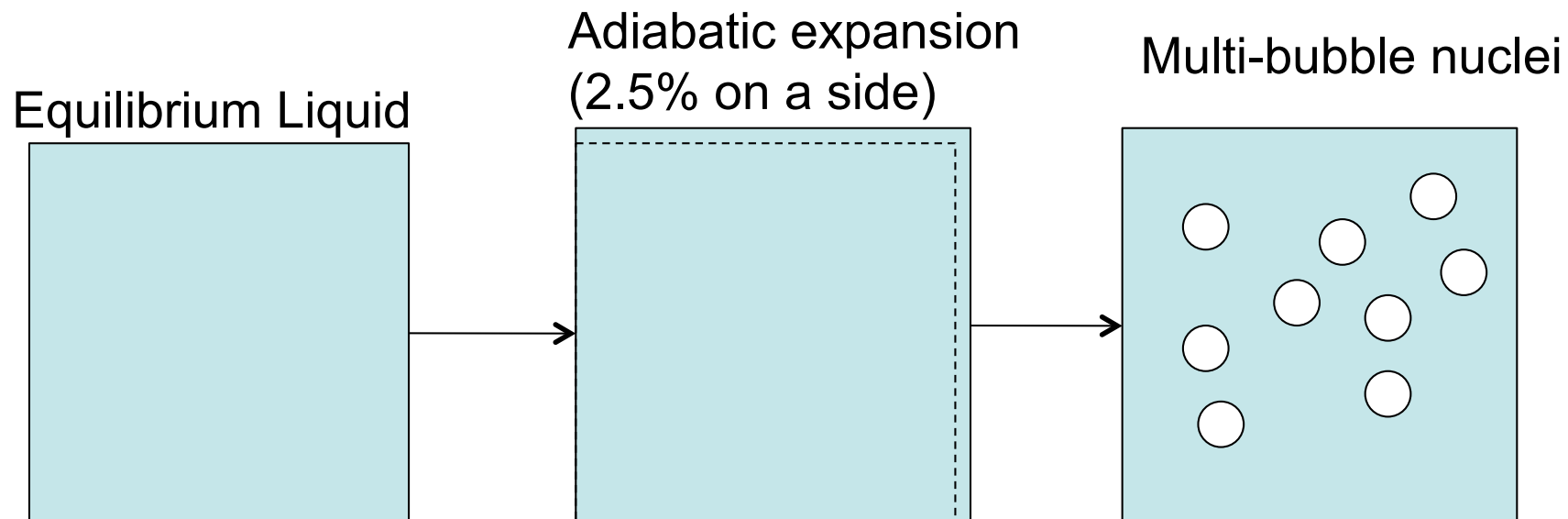
Usage of memory is almost flat for hybrid.



➔ We performed product runs using 4096 nodes adopting flat-MPI.



# Time Evolution of Multi-bubble nuclei



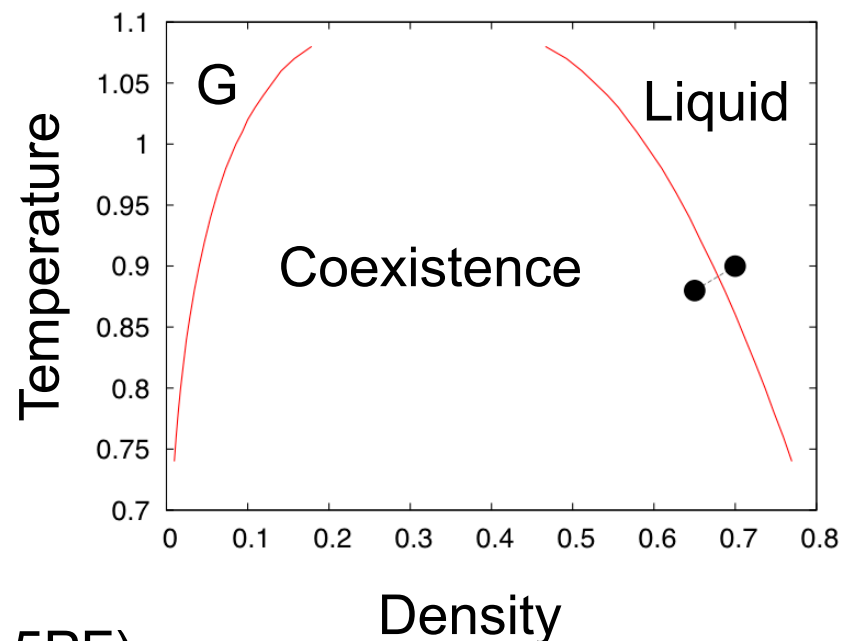
Larger bubbles becomes larger,  
smaller bubbles becomes smaller



# Details of Simulation

## Condition

Initial Condition : Pure Liquid  
 Truncation Length: 3.0  
 Periodic Boundary Condition:  
 Time Step: 0.005  
 Integration : 2<sup>nd</sup> order Symplectic (NVE)  
                   2<sup>nd</sup> order RESPA (NVT)



## Computational Scale

Resource : 4096 nodes of K computer (0.5PF)

**Flat-MPI: 32768 processes**

Parallelization: Simple Domain Decomposition

Particles: 400 ~ 700 million particles

System Size:  $L = 960$  (in LJ units)

Thermalize: 10,000 steps + Observation: 1,000,000 steps

24 hours / run

1 run ~ 0.1 million node hours

10 samples = 1 million node hours

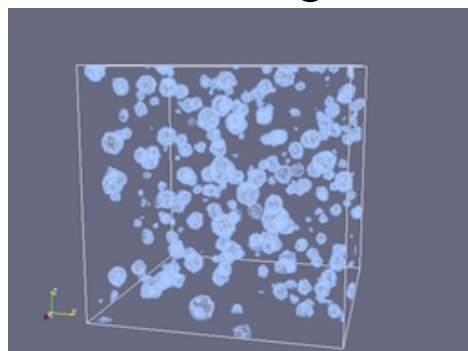
Movie



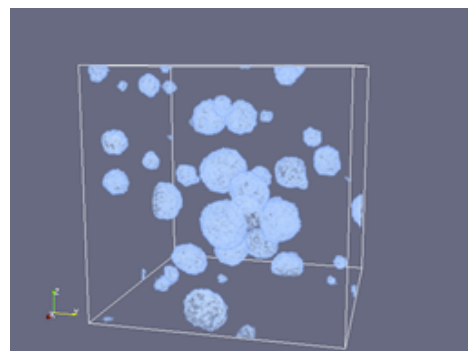
# Multi-bubble Nuclei and Ostwald-like Ripening

23 million particles

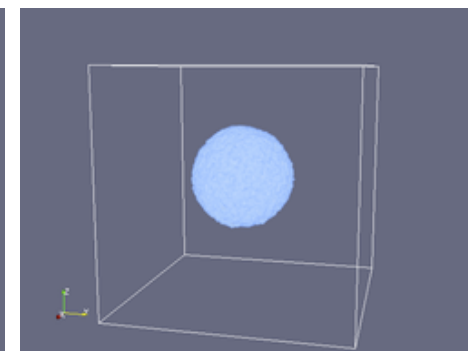
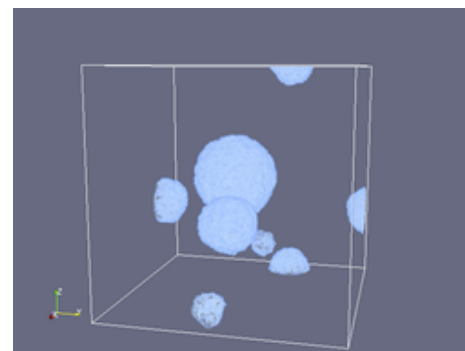
Initial stage



intermediate stage



Final stage

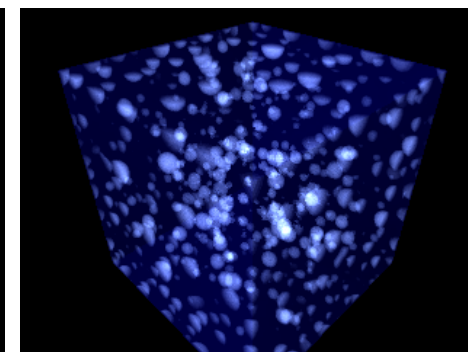
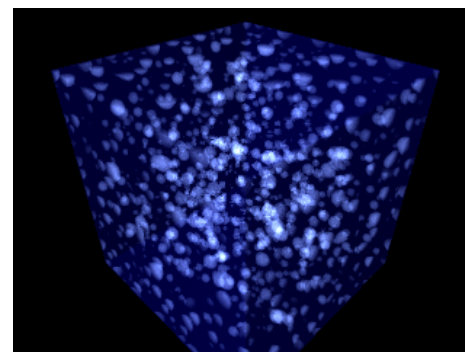
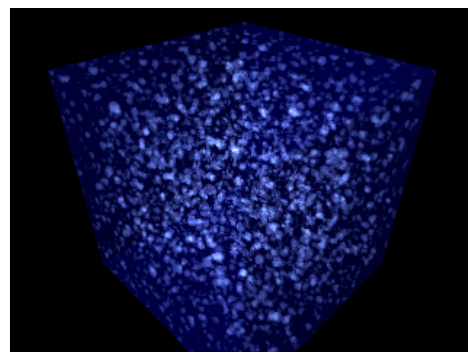
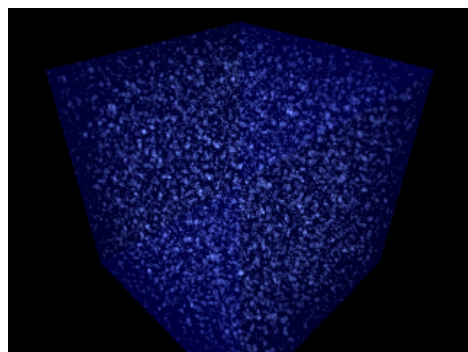


Multi nuclei

Ostwald-like ripening

One bubble survives

1.5 billion particles



Bubbles appear as the results of particle interactions.

Ostwald-like ripening is observed as the results of bubble interactions.

→ Direct simulations of multi-scale and multi-physics phenomena.



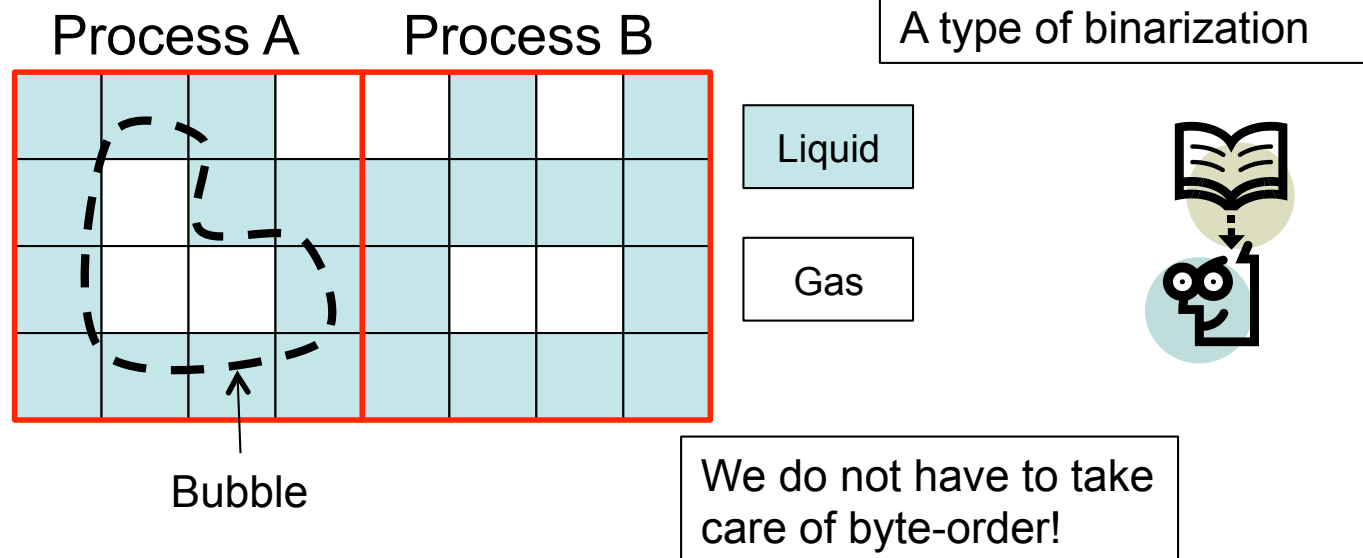
# Identification of Bubbles

## Definition of Bubble

Divide a system into small cells.

A cell with density smaller than some threshold is defined to be gas phase.

Identify bubbles on the basis of site-percolation criterion (clustering).



## Data Format

A number of particles in a cell is stored as **unsigned char** (1 Byte).

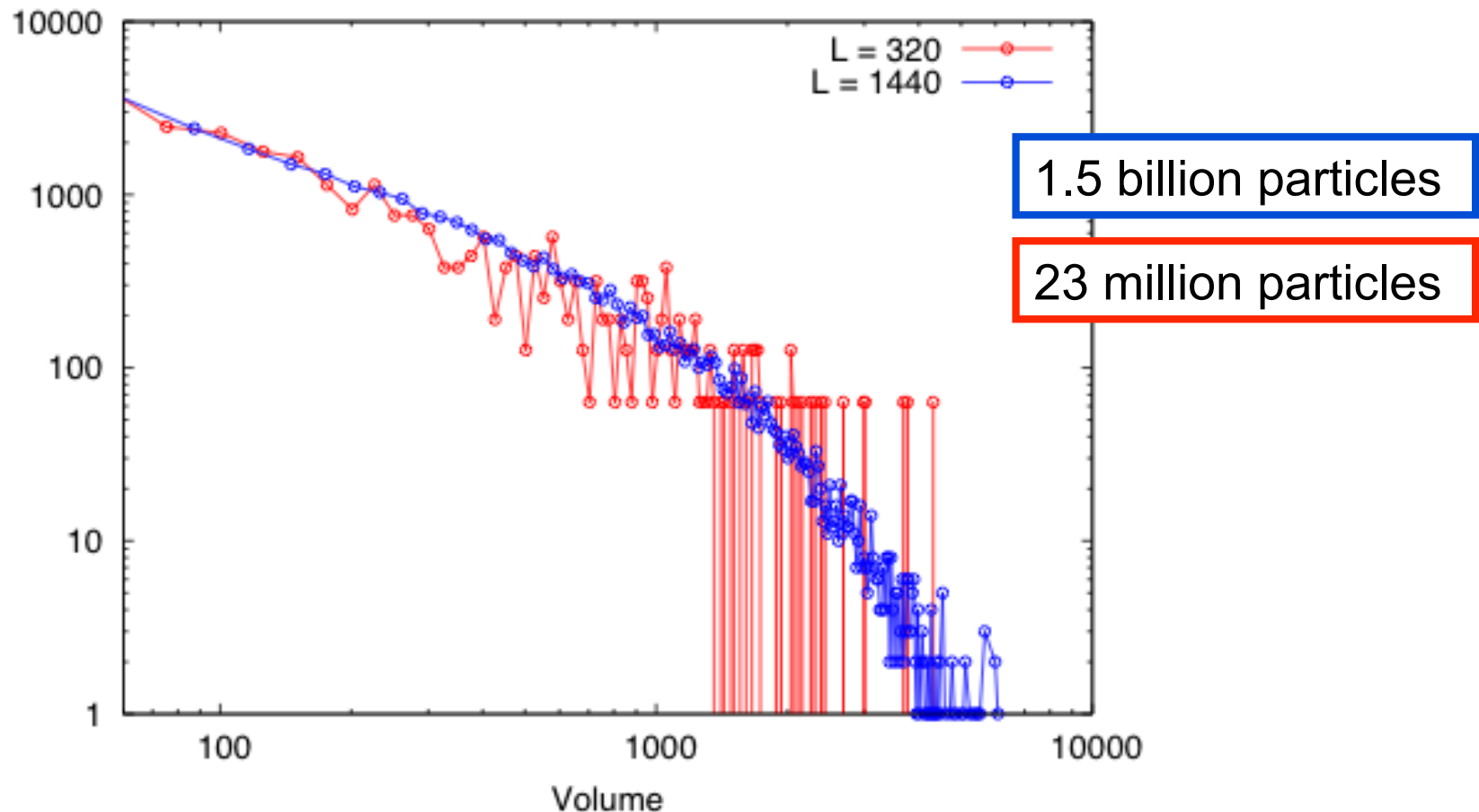
A system is divided into 32.7 million cells → 32.7 MB / snap shots.

1000 frames/run → 32.7GB/run.

Clustering is performed in post process.



# Bubble-size distribution



Bubble size distribution at the 10,000<sup>th</sup> step after the expansion.  
Accuracy of the smaller run is insufficient for further analysis.  
→ We need 1 billion particles to study population dynamics of bubbles  
which is impossible without Peta-scale computers.





# Lifshitz-Slyozov-Wagner (LSW) Theory

## Definitions

$f(v, t)$  a number of bubbles which has volume  $v$  at time  $t$ .

$$\frac{\partial f}{\partial t} = -\frac{\partial}{\partial v}(\dot{v}f) \quad \text{Governing Equation}$$

$\dot{v}(v, t)$  Kinetic Term (Microscopic Dynamics)

## Assumptions

- Mean field approximation
  - Mechanical equilibrium
  - Conservation of the total volume of gas phase
  - Self-similarity of the distribution function
- } shared with the classical nucleation theory
- $$f(v, t) \sim t^y \tilde{f}(vt^{-x})$$

## Predictions

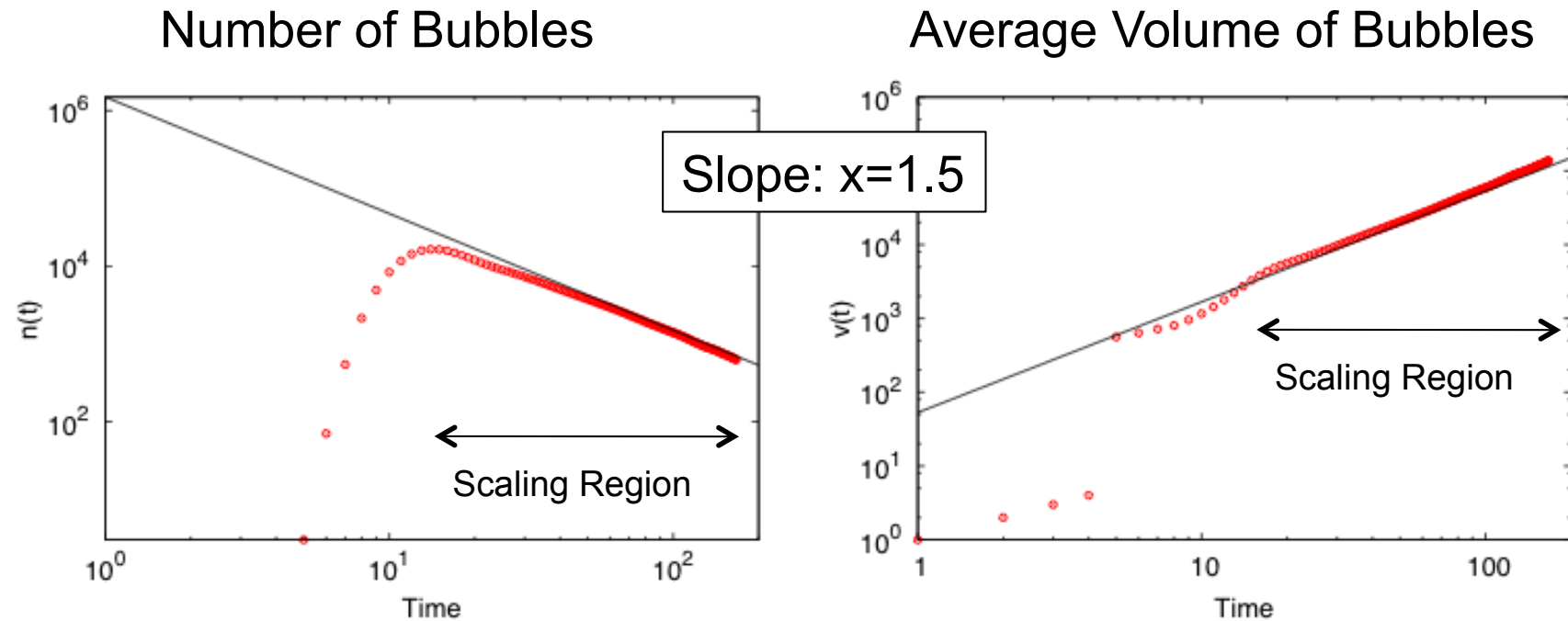
Power-law behaviors

$n(t) \sim t^{-x}$	The total number of bubbles
$\bar{v}(t) \sim t^x$	The average volume of bubbles

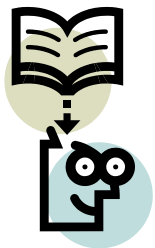
The scaling index  $x$  depends on microscopic dynamics.



# Simulations Results (1/2)



Power-law behavior in late-stage of time evolution.  
Sharing the value of an exponent as predicted by the theory.



The LSW theory works fine.

➔ Assumptions are valid.

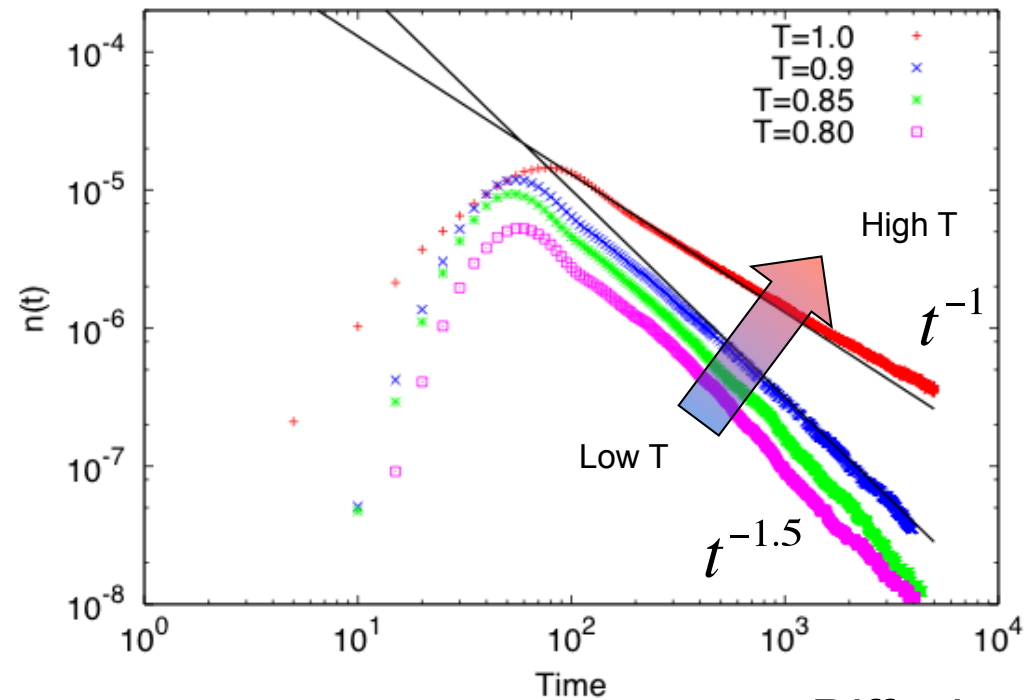
We cannot obtain the scaling region using small systems.

➔ Huge-scale simulation is necessary.



# Simulations Results (2/2)

Scaling exponent changed from 1.5 to 1



Reaction-Limit

$$\dot{v} \propto R^2 \Delta\mu$$

➔  $\chi=3/2$

Diffusion-Limit

$$\dot{v} \propto R^2 J = DR^2 \left. \frac{d\rho}{dr} \right|_{r=R}$$

➔  $\chi=1$

Microscopic dynamics can be investigated from macroscopic behavior.



# Summary and Discussion

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## Summary

We did physics using a peta-scale computer.

Simulations involving billions of particles allows us to investigate multi-scale and multi-physics problems directly.

## Toward Exa-scale Computing

Please give us decent programming language!

MPI (library), OpenMP (directive), SIMD (intrinsic functions)

## References

MDACP (Molecular Dynamics code for Avogadro Challenge Project)

Source codes are available online: <http://mdacp.sourceforge.net/>



## Acknowledgements

### **Computational Resources:**

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