

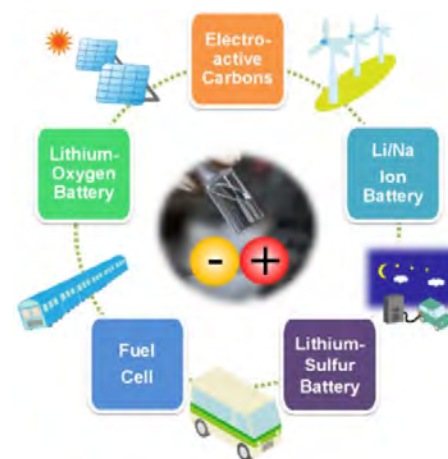
# Coarse-grained Force Field Development of Room Temperature Ionic Liquids

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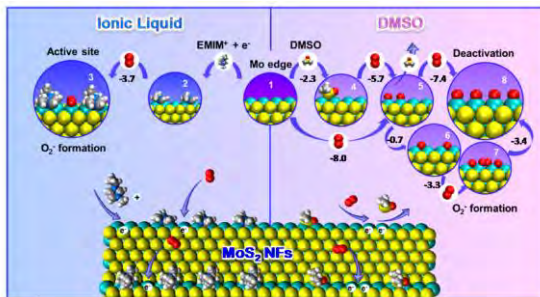
# Introduction and Background

- Room Temperature Ionic Liquid (RTIL) are a new class of solvents
- Future chemistry demands its own solvents, RTILs are known as ‘green solvent’ and ‘designer solvent’
- Potential applications are hindered by lack of fundamental understanding like their heterogeneous structure and dynamics but still in liquid phase
- Current applications include but not limited:
  1. Energy storage
  2. Gas separation
  3. Lubrication
  4. CO2 Reduction

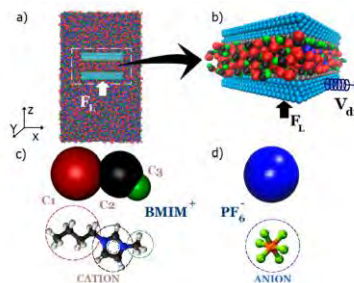


Watanabe et al. 2017 Chemical Review

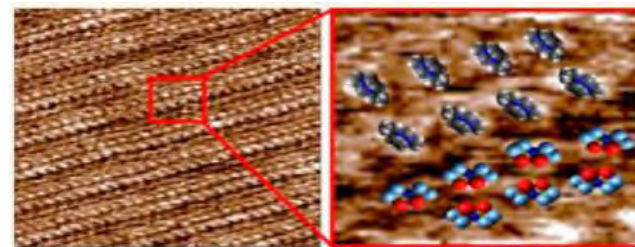
Assadi et al. 2016 ACS Nano



Fajardo et al. 2015 JCPL



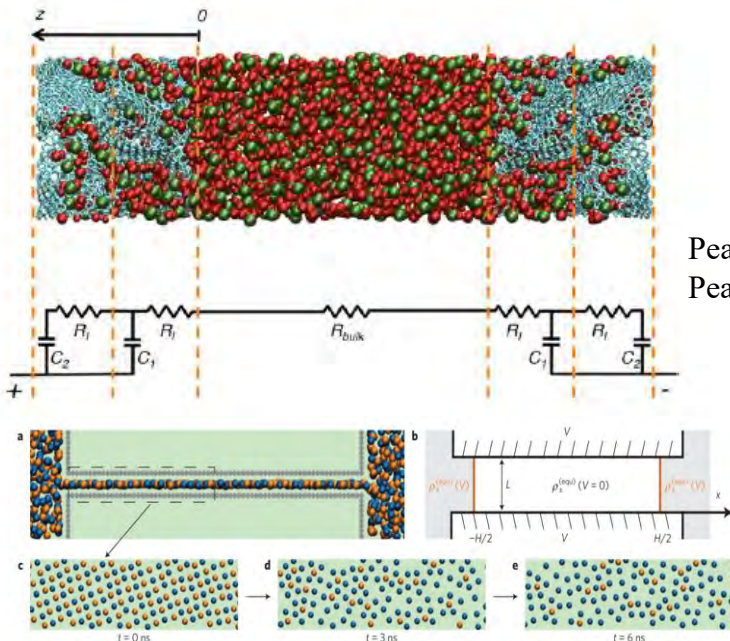
Elbourne et al. 2015 ACS Nano



# Why: Coarse-graining

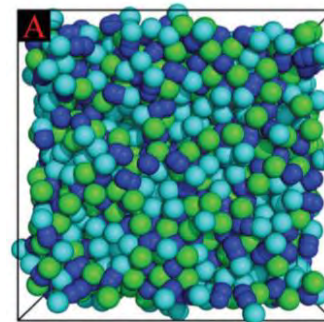
## ➤ Coarse-grained Simulation

To obtain the physical phenomena occurring in large time and size scale, hundreds of computationally intensive simulations are needed to be carried out. All-atom MD simulation is not an option. Initial study used toy model, systematically parametrized coarse-grained model can bring a breakthrough.

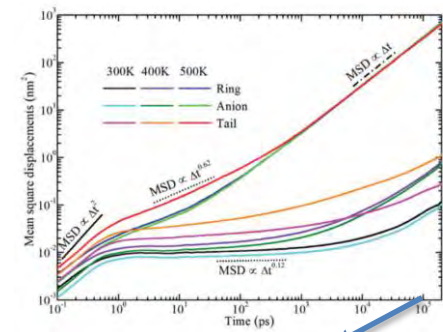


Kondrat et al. 2014 Nature Materials

Pean et al. 2014 ACS Nano  
Pean et al. 2015 JACS



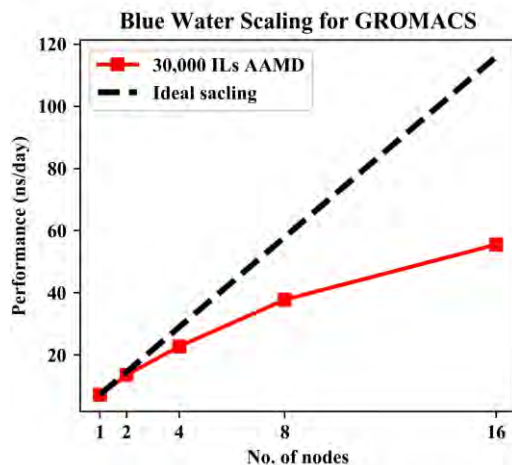
Wang et al. 2018 Soft Matter,



~100 ns

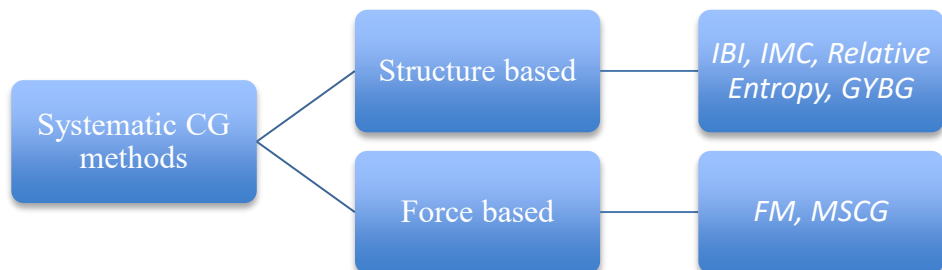
# System: Coarse-Grained and All-atom Simulations

- System size for all-atom (AA) and coarse-grained (CG) simulation and cases, without computational cost of force field optimization!
- Package
  1. GROMACS (MD) (Parallel)
  2. VOTCA (data analyzing, Los Alamos National Laboratory)
 (Multi-thread, 32 Threads of BW, makes it really fast)
- Scalability of GROMACS



System	Type	Size	Cases	Time
$C_4MIM$	AA	24000	10	50 ns
$C_6MIM$	AA	25000	2	20 ns
$C_8MIM$	AA	26000	10	50 ns
$C_{10}MIM$	AA	28000	2	20 ns
$C_4MIM$	CG	4000	1000	5 ns
$C_6MIM$	CG	4000	4	20 ns
$C_8MIM$	CG	4000	500	5 ns
$C_{10}MIM$	CG	4000	4	20 ns
Weighted average		~ 4500		9 $\mu$ s

# Introduction and Background



## ➤ Relative Entropy

Use information theory to connect all-atom and coarse-grained systems

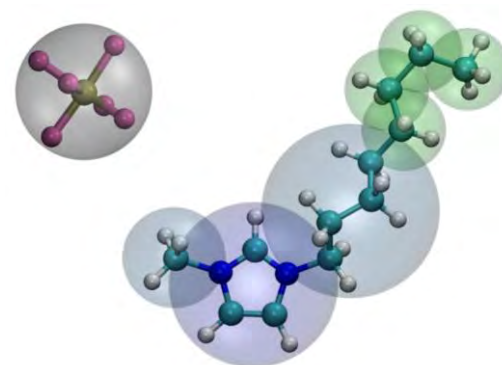
1. Systematic Charge Optimization
2. Thermodynamic Properties by adding constraint

$$S_{rel} = \beta \langle U_{CG} - U_{AA} \rangle_{AA} - \beta \langle A_{CG} - A_{AA} \rangle_{AA} + \langle S_{map} \rangle_{AA}$$

$$\nabla_{\lambda} S_{rel} = \beta \left\langle \frac{\partial U_{CG}}{\partial \lambda} \right\rangle_{AA} - \beta \left\langle \frac{\partial U_{CG}}{\partial \lambda} \right\rangle_{CG}$$

$$\lambda^{k+1} = \lambda^k - \chi H_{S_{rel}}^{-1} \cdot \nabla_{\lambda} S_{rel}$$

$$H_{ij, S_{rel}} = \beta \left\langle \frac{\partial^2 U_{CG}}{\partial \lambda_i \partial \lambda_j} \right\rangle_{AA} - \beta \left\langle \frac{\partial^2 U_{CG}}{\partial \lambda_i \partial \lambda_j} \right\rangle_{CG} + \beta^2 \left\langle \frac{\partial U_{CG}}{\partial \lambda_i} \frac{\partial U_{CG}}{\partial \lambda_j} \right\rangle_{CG} - \beta^2 \left\langle \frac{\partial U_{CG}}{\partial \lambda_i} \right\rangle_{CG} \left\langle \frac{\partial U_{CG}}{\partial \lambda_j} \right\rangle_{CG}$$

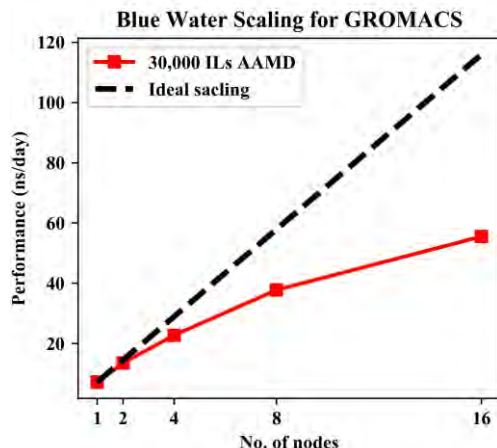


# Why: Blue Waters for Coarse-graining

- BW nodes provide sufficiently high computational memory and power, at the request or with limited queue time
- BW provides rigorous platform for data processing

32 threads for VOTCA, data processing compared to 16 on common clusters

Electrostatic interaction are long-range, so computational study demands PME algorithms to be computed efficiently.



Node	Peak Memory GB/s
Blue Water Cray XE	102
NICS Kraken Cray XT	25.6
NERSC Hopper XE	85.3
ANL IBM BG/Q	42.6

# Results: Mapping and Potential Parameters

For typical RTIL like BMIM PF6 with crude approximation for interaction between just one pair of Cation and Anion

# Non-bonded:  $\binom{32}{2} = 496$       # Bond: 32    # Angle: 45    # Dihedral: 59

Note: Consider number of atoms involved for angle (3) and dihedral (4) interaction

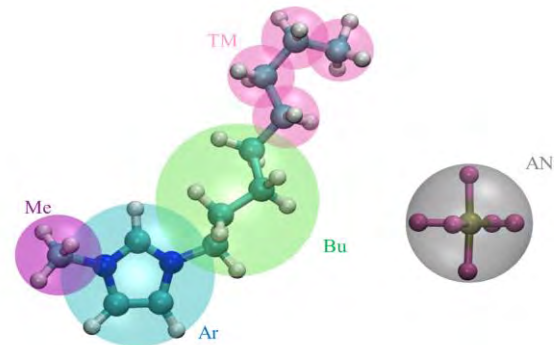
MD simulation details: (NPT ensemble) Annealing (5 ns, T = 600 K) , Equilibrium (15 ns, T = 400 K), Production (35 ns, T = 400 K )

$$u_{LJ}(r) = \frac{C_{12}}{r^{12}} - \frac{C_6}{r^6}$$

$$u_{Coul}(r_{ij}) = A_c \frac{q_i q_j}{4\pi\epsilon_0 r_{ij}}$$

Obtaining optimal parameters need hundreds of iterations of MD simulation and relative entropy optimization

$$u_{sp}(r) = [1 \quad t \quad t^2 \quad t^3] \frac{1}{6} \begin{bmatrix} 1 & 4 & 1 & 0 \\ -3 & 0 & 3 & 0 \\ 3 & -6 & 3 & 0 \\ -1 & 3 & -3 & 1 \end{bmatrix} \begin{bmatrix} C_j \\ C_{j+1} \\ C_{j+2} \\ C_{j+3} \end{bmatrix}$$



# Results: Radial Distribution Function Bead-Bead

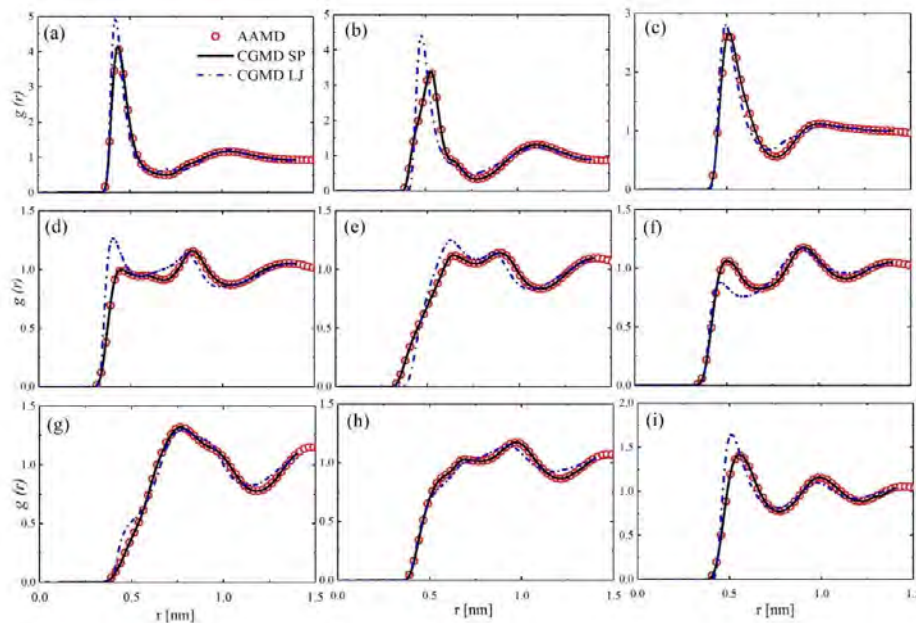
- Hierarchical Map: Moving from  $C_4C_1IM$  to  $C_8C_1IM$

$C_4$  has 10 interactions

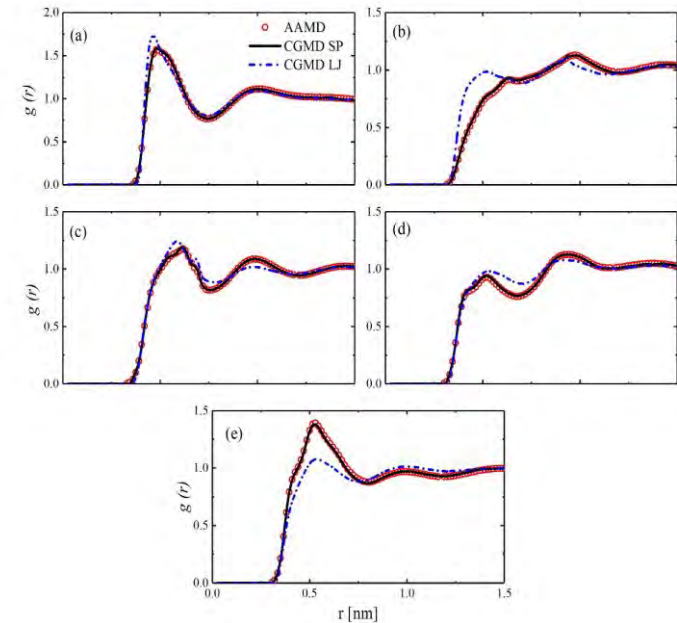
$C_8$  has 15 interactions

10 Out of 15 interactions are present in  $C_4$  so optimization is done for 5 interaction

$C_4MIM$



$C_8MIM$



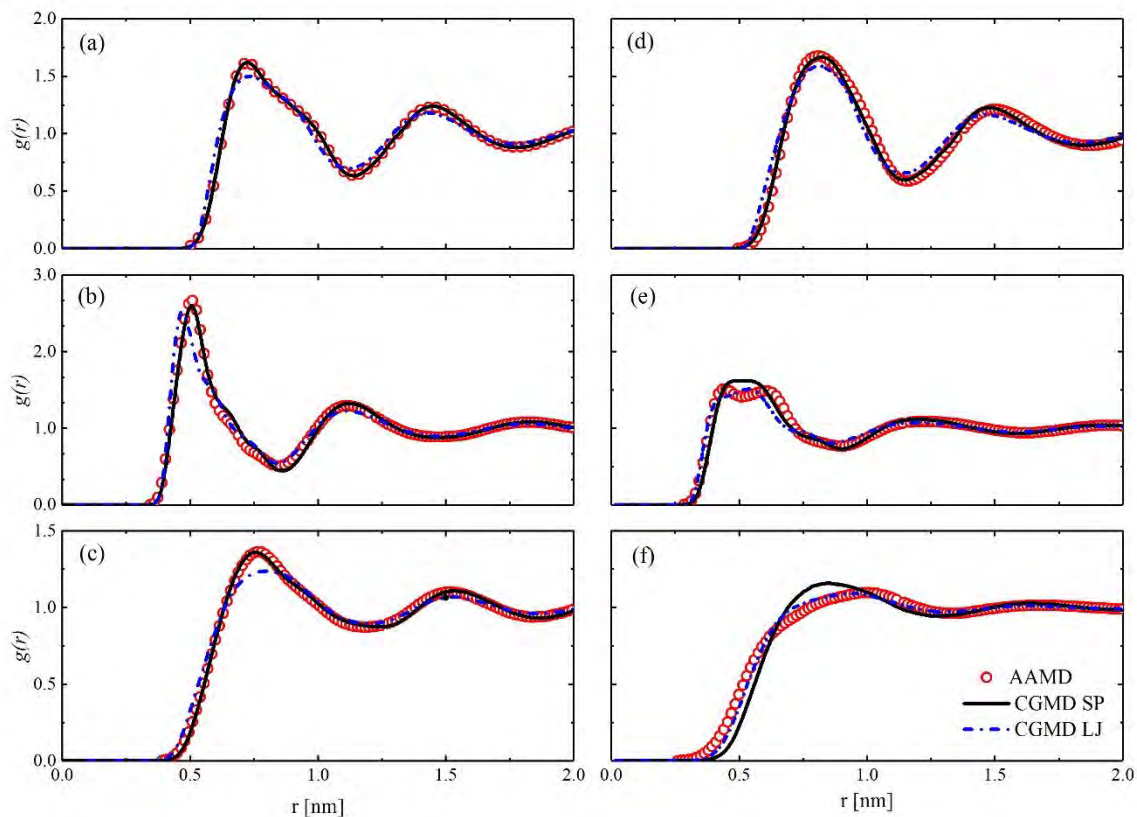


# Results: Radial Distribution Function Center of Mass

$C_4MIM$

$C_8MIM$

- Anion-Anion
- Anion-Cation
- Cation-Cation



# Results: Charge-Ordering and Screening

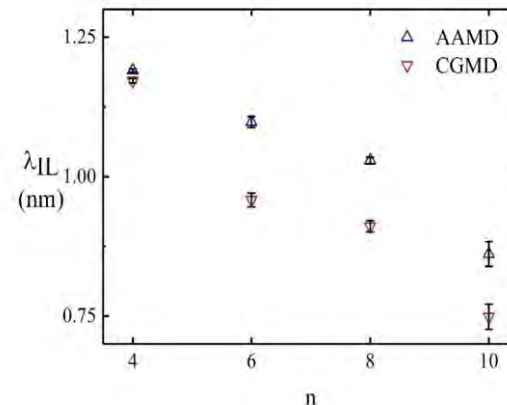
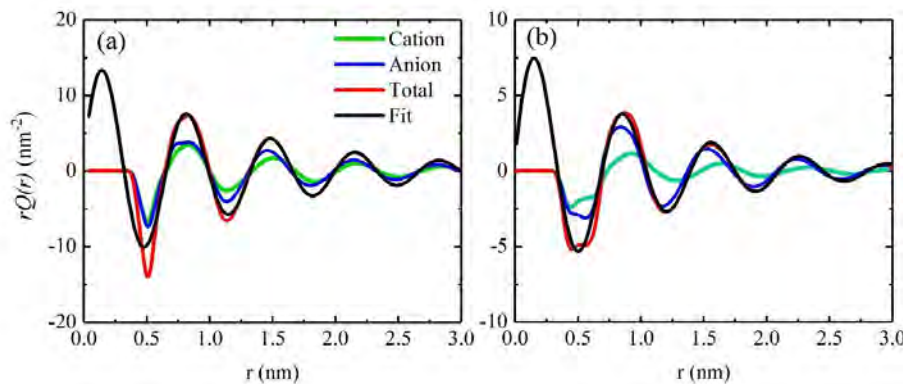
- Ionic liquids are mostly composed of charged species, how long charge-ordering goes is not well-understood. Application: touch screen, supercapacitor
- Charge-ordering and screening length depend on radial distribution function *i.e.* structure
- $\lambda_{IL}$  is screening length

$$Q^{CA}(r) = \rho(g^{CA-CA}(r) - g^{CA-AN}(r))$$

$$Q^{AN}(r) = \rho(g^{AN-AN}(r) - g^{CA-AN}(r))$$

$$Q(r) = Q^{CA}(r) + Q^{AN}(r)$$

$$Q(r) = \frac{A}{r} e^{-r/\lambda_{IL}} \sin\left(\frac{2\pi r}{d} + \psi\right)$$



# Results: Thermodynamic Properties

## Transferability in temperature

$T$ (K)	$C_4C_1IM PF_6, \rho$ ( $nm^{-3}$ )			$C_8C_1IM PF_6, \rho$ ( $nm^{-3}$ )		
	AAMD	CGMD SP	CGMD LJ	AAMD	CGMD SP	CGMD LJ
300	2.89	2.82 (2.31%)	2.93 (1.51%)	2.20	2.13 (3.18%)	2.22 (0.91%)
350	2.80	2.76 (1.21%)	2.81 (0.44%)	2.13	2.09 (1.88%)	2.14 (0.47%)
<b>400</b>	<b>2.71</b>	<b>2.71 (0.00%)</b>	<b>2.69 (0.6%)</b>	<b>2.05</b>	<b>2.05 (0.00%)</b>	<b>2.05 (0.00%)</b>
450	2.62	2.65 (1.14%)	2.58 (1.64%)	1.98	2.01 (1.52%)	1.97 (0.51%)

## Transferability for different alkyl chain lengths

$C_nC_1IM PF_6$	$n$	4	6	8	10
AAMD	Density	<b>2.71</b>	2.33	<b>2.05</b>	1.75
CGMD SP	Density	<b>2.71</b>	2.27	<b>2.05</b>	1.77
	Relative error	<b>(0.00%)</b>	(2.64%)	<b>(0.00%)</b>	(1.14%)
CGMD LJ	Density	<b>2.69</b>	2.26	<b>2.05</b>	1.78
	Relative error	<b>(0.6%)</b>	(3.00%)	<b>(0.00%)</b>	(1.71%)

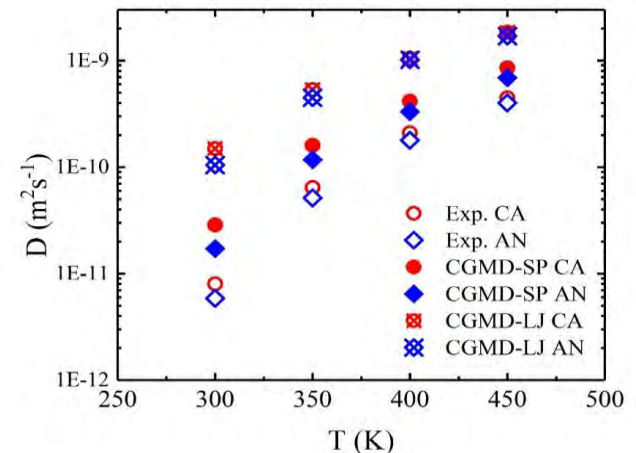
# Results: Dynamical Properties

1. Due to high charge concentration RTILs have a very slow dynamics
2. Non-polarizable all-atom force fields fail to reproduce experimental results by an order of magnitude slower dynamics, polarizable force fields are computationally expensive

Testing Current Coarse-grained force fields:

1. Diffusion coefficient is two to five times higher than experiments
2. Qualitative behavior of dynamics is preserved during coarse-graining

Bulky cation moves faster than small anion



# Conclusions and Acknowledgment

- I. Development of a systematic method for coarse-grained force fields of ionic liquid with systemic accounting for charge optimization
- II. Transferability of coarse-grained force field is analyzed for Imidazolium-based ionic liquids with different alkyl chain lengths at various thermodynamic states
- III. Charge ordering and screening analyzed for all-atom and coarse-grained model, which shed lights on recent experimental discovery regarding screening and long-range interactions in ionic liquid
- IV. Coarse-grained force field preserves the qualitative dynamical properties

**Without Blue Waters, this was not possible, Special Thanks!**



**Any Questions?**  
**Thank you for your attention**