# Simulations of Ribosome Biogenesis on the Whole Cell Level

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# **Biological Modeling at Different Scales**

Biomolecular interactions span many orders of magnitude in space and time



Whole Cells and Colonies

## **Probability of Cellular State** Algorithms for Stochastic Dynamics

<u>Chemical Master Equation – Well-stirred system (Gillespie SSA)</u>

$$\frac{dP(\vec{x},t)}{dt} = \sum_{r}^{R} -a_{r}(\vec{x})P(\vec{x},t) + a_{r}(\vec{x}-\vec{s}_{r})P(\vec{x}-\vec{s}_{r},t)$$

• <u>Reaction-Diffusion Master Equation (RDME)</u> Crowded noisy cell Exp. Baumeister, Ortiz, Xie, Elf, Moerner, Ha, Woodson, Williamson, Kuhlman  $\int_{1}^{1} \frac{dP(\vec{x},t)}{dt} = \sum_{v \in V} \sum_{r=1}^{R} -a_r(\vec{x}_v)P(\vec{x},t) + a_r(\vec{x}_v - \vec{s}_r)P(\vec{x} - \vec{s}_r \mathbf{1}_v, t)$   $+ \sum_{i \in V} \sum_{j \in V} \sum_{\alpha=1}^{N} -d_{ij}^{\alpha} x_i^{\alpha} P(\vec{x},t) + d_{ji}^{\alpha} (x_j^{\alpha} + \mathbf{1}_j^{\alpha})P(\vec{x} + \mathbf{1}_j^{\alpha} - \mathbf{1}_i^{\alpha}, t)$ 

Exp. proteomics

Heterogeneous cellular environment – 50% volume packed with macromolecules

# **Challenging Cell Simulations & Experiments**

Stochastic Gene Expression Switching Cells

INVIDIA EFORCE GTX

mRNA

Operon

Protein

Ribosome

а

0.9 µm

Metabolic Response in Colony of Cells ~2000 metabolic rxns

Oxygen

4



# Cell Simulations with Lattice Microbes



- Molecular crowding & protein/RNA distributions
- (CET, SM, RNA seq & proteomics data)
- Reactions as RDME solved on 3D lattice for cell cycle using Multi GPUs
- Kinetic parameters < biochem & SM experiments – e.g.sRNA, ribosome biogenesis
- Population FBA: Steady-state fluxes through thermodynamically balanced cellular networks and growth rate distributions – E. coli and Yeast
- Hybrid RD(ME)/FBA models Cell Colonies

Roberts, ... ZLS (2009,2011,2013) *IEEE*, *PLoS CB, JCC* Earnest, ... ZLS *Phys.Bio* (2012),Assaf,... (2012,2013) *PRL* \*Labhsetwar, Cole, ... ZLS, (2013) *PNAS* \*Cole, ... ZLS,in *Comp. Sys. Bio.* (2014) \*Hallock,... *Par. Comp.* (2014), Peterson,... *PyHPC* 2013 \* Cole,... ZLS, *Israel J. Chem*, 2014, *BMC Sys. Bio.* (2015) \*Earnest,... Williamson, ZLS, *BPJ* (submitted 2015)

## Molecular Signatures in Evolution of Translation Kinetic Model Ribosome Biogenesis



Universal Phylogenetic Tree



Dynamical function of ribosomal signatures: idiosyncrasies in ribosomal RNA and/or proteins characteristic of the domains of life

Roberts, ... Woese, Luthey-Schulten (2008) *PNAS*; Chen,... Gruebele, Luthey-Schulten (2010) *BJ* Chen, ...Ha, Woodson, Luthey-Schulten, (2012) *JPCB*; Lai, Chen, Luthey-Schulten (2013) *JPCB* Kim,... Luthey-Schulten Z., Ha, and Woodson (2014) *Nature* "Protein-guided RNA dynamics during early ribosome assembly"

# From in vitro Assembly Model to Biogenesis

#### 16S rRNA + 20 SSU proteins = 2<sup>20</sup> states

Nomura Hierarchical Map >>> 1612 states



## Comparison of full to reduced kinetic model – 40<sup>0</sup> C

Pulse Chase experiments - Control Experiments - Williamson, Science 2010, Elife 2014



Earnest, Lai, Chen, Hallock, Williamson, Luthey-Schulten (submitted, 2015)

# In vivo ribosome assembly on Blue Waters



# In silico Ribosome Biogenesis\*



## Experimental Data on Operon and Ribosome Distributions

#### **Ribosome Distributions**



#### Expression levels in exp. growth



#### Distribution from CET in LM Simulations



# Improving Multi-GPU Performance



- Single GPU performance improved 2.5x 3x from Fermi (2070) to Kepler (K40)
- Parallel efficiency improves for small simulations due to better host system topology and higher-performance inter-GPU communication
- Today -1 cell cycle simulation (~2 hours) of 1200 rxns, 255 species in ribosome biogenesis - 3 days with JIT code using GTX980 (Cuda 6.5) and 6 days (K20,Cuda 5x)

# Reaction Kernel Code Generation Performance – 1200 Rxns, 255 species



## Future Goal: Reduced Models of All Cellular Networks



## **Competition for Resources in Bacterial Colonies**



## 3D Dynamical FBA Method (3DdFBA) for Cell Colonies



neighboring sites with lower cell density

## Substrate Gradients Drive Metabolic Differentiation





#### **Experimental Metabolic Behavior**

## Substrate Gradients Drive Metabolic Differentiation

#### Optical Sectioning: Near base, oxygen-starved cells consume glucose and produce acetate

Predicted Metabolic Behavior

#### Glucose Acetate Production & Glucose Consumption Building Acetate Consumption Acetate Consumption Building Acetate Consumption Consumption

# 200 µm 150 µm 100 µm 50 µm GFP mCherry Composite (Glucose) (Acetate)

#### **Experimental Metabolic Behavior**

### Substrate Gradients Drive Metabolic Differentiation

Near colony top, glucose-starved cells consume acetate. OS and side views confirm predictions.

Predicted Metabolic Behavior 1 mm Agar Glucose Acetate Consumption Acetate Production & Glucose Consumption Malate Synthase Acetvl-CoA Isocitrate Acetate Synthase Lyase Acetate



**Experimental Metabolic Behavior** 



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M. Gruebele Carl Woese 2012





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**Center for the Physics** 

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NIH Center - Beckman Inst.

VMD, NAMD, LM

of Living Cells

#### NCSA BW & XSEDE







#### Max Planck Institute FIB milling of cells





E. VILLA UCSD Joe Peterson, Seth Thor







W. Baumeister, J. Ortíz



John Stone



Mike Hallock, Fry,



Marcelo Melo